

# Package: millsratio (via r-universe)

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**Title** Interactive Analysis of Mills Ratios and Tail Thickness

**Version** 0.2.3

**Description** Compute and compare Mills ratios for normal, t, and exponential distributions. Explore the t(30) paradox where heavier tails produce larger Mills ratios despite near-normal density. Includes an interactive Shiny dashboard for visualising tail behaviour and hazard functions.

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analyze\_t30\_paradox    *Generate Data for t(30) Paradox Analysis*

---

### Description

Generate Data for t(30) Paradox Analysis

### Usage

```
analyze_t30_paradox(x_range = c(0, 5), n_points = 200)
```

### Arguments

x_range	Range of x values
n_points	Number of points

**Value**

Data frame comparing t(30) and normal distributions

**Examples**

```
paradox_data <- analyze_t30_paradox()
```

---

```
analyze_tail_thickness
```

*Analyze Tail Thickness at Specific Points*

---

**Description**

Analyze Tail Thickness at Specific Points

**Usage**

```
analyze_tail_thickness(  
  x_points,  
  distributions = c("normal", "t30", "exponential"),  
  compute_ratios = FALSE  
)
```

**Arguments**

`x_points` Numeric vector of x values to analyze  
`distributions` Character vector of distributions  
`compute_ratios` Logical; if TRUE, computes ratios relative to normal

**Value**

Data frame with Mills ratios and optional comparison metrics

**Examples**

```
# Analyze at key points  
tail_analysis <- analyze_tail_thickness(  
  x_points = c(2, 3, 4, 5),  
  distributions = c("normal", "t30", "exponential"),  
  compute_ratios = TRUE  
)
```

---

compare\_mills\_hazard *Compare Mills Ratio and Hazard Function*

---

## Description

Compare Mills Ratio and Hazard Function

## Usage

```
compare_mills_hazard(x, distribution = "normal", ...)
```

## Arguments

x	Numeric vector of values
distribution	Character string specifying distribution
...	Additional distribution parameters

## Value

Data frame with x, mills\_ratio, and hazard columns

## Examples

```
# Compare for normal distribution
compare_mills_hazard(seq(0, 5, by = 0.5), "normal")

# Tidyverse visualization
library(dplyr)
library(ggplot2)
compare_mills_hazard(seq(0.1, 5, by = 0.1), "normal") %>%
  tidyr::pivot_longer(c(mills_ratio, hazard),
                     names_to = "function_type",
                     values_to = "value") %>%
  ggplot(aes(x, value, color = function_type)) +
  geom_line() +
  scale_y_log10() +
  labs(title = "Mills Ratio vs Hazard Function",
       subtitle = "Note: h(x) = 1/m(x)")
```

---

compare\_mills\_ratios    *Compare Mills Ratios Across Distributions*

---

**Description**

Compare Mills Ratios Across Distributions

**Usage**

```
compare_mills_ratios(x, distributions = c("normal", "t30", "exponential"))
```

**Arguments**

x	Numeric vector of quantiles
distributions	Character vector of distribution names ("normal", "t3", "t10", "t30", "exponential")

**Value**

Data frame with Mills ratios for each distribution

**Examples**

```
x_vals <- c(1, 2, 3, 4)
compare_mills_ratios(x_vals, c("normal", "t30", "exponential"))
```

---

dashboard\_about    *Get Dashboard About Information*

---

**Description**

Get Dashboard About Information

**Usage**

```
dashboard_about()
```

**Value**

List with dashboard metadata

---

find\_crossover\_point *Find Crossover Points Between Distributions*

---

## Description

Find Crossover Points Between Distributions

## Usage

```
find_crossover_point(  
  dist1,  
  dist2,  
  df1 = NULL,  
  df2 = NULL,  
  x_range = c(0.01, 10),  
  tolerance = 1e-06  
)
```

## Arguments

dist1	First distribution
dist2	Second distribution
df1	Degrees of freedom for first distribution (if t)
df2	Degrees of freedom for second distribution (if t)
x_range	Search range for crossover
tolerance	Numerical tolerance for finding crossover

## Value

Numeric value of x where Mills ratios are equal (NA if no crossover)

## Examples

```
# Find where t(30) and normal Mills ratios cross  
crossover <- find_crossover_point("t", "normal", df1 = 30)
```

---

hazard_from_mills	<i>Convert Mills Ratio to Hazard Function</i>
-------------------	---

---

**Description**

Convert Mills Ratio to Hazard Function

**Usage**

```
hazard_from_mills(mills_ratio)
```

**Arguments**

mills\_ratio      Numeric vector of Mills ratio values

**Value**

Numeric vector of hazard function values

**Examples**

```
# Normal distribution example
x <- seq(0, 5, by = 0.5)
m <- mills_ratio_normal(x)
h <- hazard_from_mills(m)

# Tidyverse example
library(dplyr)
data.frame(x = x) %>%
  mutate(
    mills = mills_ratio_normal(x),
    hazard = hazard_from_mills(mills)
  )
```

---

hazard_function	<i>Calculate Hazard Function Directly</i>
-----------------	---

---

**Description**

Calculate Hazard Function Directly

**Usage**

```
hazard_function(x, distribution = "normal", ...)
```

**Arguments**

x                    Numeric vector of values  
 distribution        Character string: "normal", "t", "exponential"  
 ...                    Additional parameters for the distribution

**Value**

Numeric vector of hazard function values

**Examples**

```
# Compare hazard functions across distributions
x <- seq(0.1, 5, by = 0.1)
h_normal <- hazard_function(x, "normal")
h_t30 <- hazard_function(x, "t", df = 30)
h_exp <- hazard_function(x, "exponential", rate = 1)

# Tidyverse comparison
library(dplyr)
library(tidyr)
data.frame(x = x) %>%
  mutate(
    Normal = hazard_function(x, "normal"),
    `t(30)` = hazard_function(x, "t", df = 30),
    Exponential = hazard_function(x, "exponential")
  ) %>%
  pivot_longer(-x, names_to = "distribution", values_to = "hazard")
```

---

hazard\_functions                    *Hazard Function Calculations*

---

**Description**

Functions for calculating hazard functions and their relationship to Mills ratios. The hazard function  $h(x) = f(x)/(1-F(x))$  is the reciprocal of the Mills ratio  $m(x)$ .

**Details**

The hazard function (also called failure rate or force of mortality) represents the instantaneous rate of occurrence of an event at time  $x$ , given survival to time  $x$ .

Mathematical relationship:  $h(x) = 1/m(x)$

---

hazard_properties	<i>Hazard Function Properties</i>
-------------------	-----------------------------------

---

**Description**

Analyze properties of the hazard function for different distributions.

**Usage**

```
hazard_properties(distribution = "normal", df = NULL)
```

**Arguments**

distribution	Character string: "normal", "t", or "exponential"
df	Degrees of freedom for t-distribution

**Value**

List with hazard function properties

**Examples**

```
# Analyze normal distribution hazard
hazard_properties("normal")

# Compare properties across distributions
library(purrr)
list(
  normal = hazard_properties("normal"),
  t30 = hazard_properties("t", df = 30),
  exponential = hazard_properties("exponential")
) %>%
  map_df(~ as.data.frame(.x), .id = "distribution")
```

---

launch_dashboard	<i>Launch Mills Ratio Interactive Dashboard</i>
------------------	---

---

**Description**

Launches an interactive Shiny dashboard for exploring Mills ratios and tail thickness behavior across different distributions.

**Usage**

```
launch_dashboard(port = NULL, launch_browser = TRUE, host = "127.0.0.1")
```

**Arguments**

port	Port number for the Shiny app (default = NULL for auto-selection)
launch_browser	Logical; if TRUE, opens dashboard in browser
host	Host address (default = "127.0.0.1" for local access)

**Value**

Runs the Shiny application

**Examples**

```
## Not run:  
# Launch the dashboard  
launch_dashboard()  
  
# Launch on specific port  
launch_dashboard(port = 8080)  
  
## End(Not run)
```

---

launch\_dashboard\_no\_browser

*Launch Dashboard Without Browser*

---

**Description**

Convenience function to launch dashboard without attempting to open browser. Useful when browser settings are not configured.

**Usage**

```
launch_dashboard_no_browser(port = NULL, host = "127.0.0.1")
```

**Arguments**

port	Port number for the Shiny app (default = NULL for auto-selection)
host	Host address (default = "127.0.0.1" for local access)

**Value**

Runs the Shiny application

**Examples**

```
## Not run:  
# Launch without browser  
launch_dashboard_no_browser()  
# Then manually open the displayed URL in your browser  
  
## End(Not run)
```

---

```
launch_dashboard_simple  
  Launch Simplified Dashboard
```

---

**Description**

Launch the simplified, content-focused version of the Mills ratio dashboard. This version emphasizes clarity and substance over visual effects.

**Usage**

```
launch_dashboard_simple(  
  port = 4628,  
  launch_browser = FALSE,  
  host = "127.0.0.1"  
)
```

**Arguments**

port	Port number for the Shiny app (default = 4628)
launch_browser	Launch browser? (default = FALSE)
host	Host address (default = "127.0.0.1" for local access)

**Value**

Runs the simplified Shiny application

**Examples**

```
## Not run:  
# Launch simplified dashboard  
launch_dashboard_simple()  
  
## End(Not run)
```

mills\_asymptotic      *Calculate Asymptotic Approximation of Mills Ratio*

---

**Description**

Calculate Asymptotic Approximation of Mills Ratio

**Usage**

```
mills_asymptotic(x, distribution, df = NULL)
```

**Arguments**

x	Numeric vector of quantiles
distribution	Character string: "normal", "t", or "exponential"
df	Degrees of freedom for t-distribution

**Value**

Numeric vector of asymptotic approximations

**Examples**

```
# Normal asymptotic approximation (1/x for large x)
mills_asymptotic(10, "normal")

# Student's t asymptotic approximation (x/df for large x)
mills_asymptotic(10, "t", df = 30)
```

---

mills\_ratio\_comparison      *Compute Ratio of Mills Ratios*

---

**Description**

Compute Ratio of Mills Ratios

**Usage**

```
mills_ratio_comparison(x, dist1, dist2, df1 = NULL, df2 = NULL)
```

**Arguments**

x	Numeric vector of quantiles
dist1	First distribution ("normal", "t", "exponential")
dist2	Second distribution ("normal", "t", "exponential")
df1	Degrees of freedom for first distribution (if t)
df2	Degrees of freedom for second distribution (if t)

**Value**

Numeric vector of ratios  $m1(x)/m2(x)$

**Examples**

```
# Ratio of t(30) to normal Mills ratios
x_vals <- seq(1, 5, by = 0.5)
ratio <- mills_ratio_comparison(x_vals, "t", "normal", df1 = 30)
```

---

mills\_ratio\_exp      *Compute Mills Ratio for Exponential Distribution*

---

**Description**

Compute Mills Ratio for Exponential Distribution

**Usage**

```
mills_ratio_exp(x, rate = 1, log = FALSE)
```

**Arguments**

x	Numeric vector of quantiles
rate	Rate parameter (> 0)
log	Logical; if TRUE, returns log(Mills ratio)

**Value**

Numeric vector of Mills ratios

**Examples**

```
# Exponential with rate = 1 at x = 2
mills_ratio_exp(2, rate = 1)

# Mills ratio is constant for exponential!
mills_ratio_exp(c(1, 2, 3, 4), rate = 1)
```

---

mills\_ratio\_generic    *Generic Mills Ratio Function*

---

**Description**

Generic Mills Ratio Function

**Usage**

```
mills_ratio_generic(x, cdf_fun, pdf_fun, log = FALSE, ...)
```

**Arguments**

x	Numeric vector of quantiles
cdf_fun	CDF function (must accept lower.tail and log.p arguments)
pdf_fun	PDF function (must accept log argument)
log	Logical; if TRUE, returns log(Mills ratio)
...	Additional arguments passed to cdf_fun and pdf_fun

**Value**

Numeric vector of Mills ratios

**Examples**

```
# Using generic function for normal distribution
mills_ratio_generic(2, cdf_fun = pnorm, pdf_fun = dnorm)

# Using for custom distribution
# mills_ratio_generic(x, cdf_fun = my_cdf, pdf_fun = my_pdf, param1 = value1)
```

---

mills\_ratio\_normal    *Mills Ratio Functions for Various Distributions*

---

**Description**

Functions to compute Mills ratios for different probability distributions. The Mills ratio  $m(x)$  is defined as the ratio of the complementary cumulative distribution function (CCDF) to the probability density function (PDF):  $m(x) = [1 - F(x)] / f(x)$

**Usage**

```
mills_ratio_normal(x, mean = 0, sd = 1, log = FALSE)
```

**Arguments**

x	Numeric vector of quantiles
mean	Mean of the distribution (default = 0)
sd	Standard deviation (default = 1)
log	Logical; if TRUE, returns log(Mills ratio) for numerical stability

**Value**

Numeric vector of Mills ratios

**Author(s)**

John Gavin [john.b.gavin@gmail.com](mailto:john.b.gavin@gmail.com) Compute Mills Ratio for Normal Distribution

**Examples**

```
# Standard normal Mills ratio at x = 2
mills_ratio_normal(2)

# Multiple values
mills_ratio_normal(c(1, 2, 3, 4))

# Log Mills ratio for extreme values
mills_ratio_normal(10, log = TRUE)
```

---

mills\_ratio\_t                      *Compute Mills Ratio for Student's t Distribution*

---

**Description**

Compute Mills Ratio for Student's t Distribution

**Usage**

```
mills_ratio_t(x, df, log = FALSE)
```

**Arguments**

x	Numeric vector of quantiles
df	Degrees of freedom (> 0)
log	Logical; if TRUE, returns log(Mills ratio)

**Value**

Numeric vector of Mills ratios

**Examples**

```
# t-distribution with df = 30 at x = 2
mills_ratio_t(2, df = 30)

# Compare different degrees of freedom
x_vals <- seq(0, 5, by = 0.5)
m_t3 <- mills_ratio_t(x_vals, df = 3)
m_t30 <- mills_ratio_t(x_vals, df = 30)
```

---

`monte_carlo_mills`*Monte Carlo Simulation for Mills Ratio Estimation*

---

**Description**

Monte Carlo Simulation for Mills Ratio Estimation

**Usage**

```
monte_carlo_mills(  
  n_sim = 10000,  
  x_val = 2,  
  distribution = "normal",  
  df = NULL,  
  seed = NULL  
)
```

**Arguments**

<code>n_sim</code>	Number of simulations
<code>x_val</code>	Value at which to estimate Mills ratio
<code>distribution</code>	Distribution to sample from
<code>df</code>	Degrees of freedom (for t-distribution)
<code>seed</code>	Random seed for reproducibility

**Value**

List with empirical Mills ratio estimate and confidence interval

**Examples**

```
# Empirically verify Mills ratio for normal at x=2
mc_result <- monte_carlo_mills(n_sim = 10000, x_val = 2, distribution = "normal")
```

---

plot\_mills\_comparison *Plot Mills Ratio Comparison*

---

### Description

Plot Mills Ratio Comparison

### Usage

```
plot_mills_comparison(  
  x_range = c(0, 5),  
  dist1,  
  dist2,  
  df1 = NULL,  
  df2 = NULL,  
  show_ratio = TRUE  
)
```

### Arguments

x_range	Range of x values
dist1	First distribution
dist2	Second distribution
df1	Degrees of freedom for first distribution
df2	Degrees of freedom for second distribution
show_ratio	Logical; if TRUE, shows ratio plot

### Value

ggplot2 object

### Examples

```
plot_mills_comparison(c(0, 5), "t", "normal", df1 = 30)
```

---

plot\_mills\_curves *Visualization Functions for Mills Ratio Analysis*

---

### Description

Functions to create static and interactive visualizations of Mills ratios, supporting both ggplot2 and plotly outputs.

**Usage**

```
plot_mills_curves(  
  data,  
  log_y = FALSE,  
  log_x = FALSE,  
  interactive = FALSE,  
  title = "Mills Ratio Comparison",  
  show_asymptotic = TRUE  
)
```

**Arguments**

data	Data frame from simulate_mills_curves()
log_y	Logical; if TRUE, uses log scale for y-axis
log_x	Logical; if TRUE, uses log scale for x-axis
interactive	Logical; if TRUE, returns plotly object
title	Plot title
show_asymptotic	Logical; if TRUE, shows asymptotic approximations

**Value**

ggplot2 or plotly object

**Author(s)**

John Gavin [john.b.gavin@gmail.com](mailto:john.b.gavin@gmail.com) Plot Mills Ratio Curves

**Examples**

```
# Generate and plot Mills ratio curves  
curves <- simulate_mills_curves(distributions = c("normal", "t30", "exponential"))  
plot_mills_curves(curves, log_y = TRUE)
```

---

plot\_mills\_vs\_hazard *Plot Mills Ratio vs Hazard Function Side-by-Side*

---

**Description**

Plot Mills Ratio vs Hazard Function Side-by-Side

**Usage**

```
plot_mills_vs_hazard(
  x_range = c(0.1, 5),
  distributions = c("normal", "t30", "exponential"),
  n_points = 200,
  interactive = FALSE,
  log_y = TRUE
)
```

**Arguments**

x_range	Numeric vector of length 2 giving the range of x values
distributions	Character vector of distribution names (e.g., c("normal", "t30", "exponential"))
n_points	Number of points to compute (default 200)
interactive	Logical; if TRUE, returns plotly object
log_y	Logical; if TRUE, uses log scale for y-axis

**Value**

ggplot2 or plotly object with faceted  $m(x)$  and  $h(x)$  panels

**Examples**

```
plot_mills_vs_hazard()
plot_mills_vs_hazard(x_range = c(0.5, 8), distributions = c("normal", "t30"))
```

---

plot_t30_paradox	<i>Plot t(30) Paradox Visualization</i>
------------------	---

---

**Description**

Plot  $t(30)$  Paradox Visualization

**Usage**

```
plot_t30_paradox(data, focus = "mills", interactive = FALSE)
```

**Arguments**

data	Data frame from analyze_t30_paradox()
focus	Character: "mills", "pdf", "cdf", or "all"
interactive	Logical; if TRUE, returns plotly object

**Value**

ggplot2 or plotly object

**Examples**

```
paradox_data <- analyze_t30_paradox()
plot_t30_paradox(paradox_data, focus = "mills")
```

---

```
plot_tail_thickness_heatmap
```

*Plot Tail Thickness Heatmap*

---

**Description**

Plot Tail Thickness Heatmap

**Usage**

```
plot_tail_thickness_heatmap(x_points, distributions, interactive = FALSE)
```

**Arguments**

x_points	Vector of x values
distributions	Vector of distribution names
interactive	Logical; if TRUE, returns plotly object

**Value**

ggplot2 or plotly heatmap

**Examples**

```
plot_tail_thickness_heatmap(
  x_points = seq(1, 5, by = 0.5),
  distributions = c("normal", "t3", "t10", "t30", "exponential")
)
```

---

```
simulate_mills_curves
```

*Simulation Framework for Mills Ratio Analysis*

---

**Description**

Functions to generate and compare Mills ratio curves across distributions, supporting the interactive dashboard and analysis vignettes.

**Usage**

```
simulate_mills_curves(  
  x_range = c(0.5, 5),  
  n_points = 100,  
  distributions = c("normal", "t3", "t30", "exponential"),  
  log_scale = FALSE,  
  include_asymptotic = FALSE  
)
```

**Arguments**

x_range	Numeric vector of two elements: c(min, max)
n_points	Number of points to evaluate (default = 100)
distributions	Character vector of distributions to include
log_scale	Logical; if TRUE, uses log-spaced x values
include_asymptotic	Logical; if TRUE, includes asymptotic approximations

**Value**

Data frame in long format suitable for plotting

**Author(s)**

John Gavin [john.b.gavin@gmail.com](mailto:john.b.gavin@gmail.com) Generate Mills Ratio Curves

**Examples**

```
# Generate curves for comparison  
curves <- simulate_mills_curves(  
  x_range = c(0.5, 5),  
  distributions = c("normal", "t3", "t30", "exponential")  
)
```

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